Introduction to mathematical cryptography Homework problems Week 3

- 5. Assume G is a group, and H_1, H_2 are subgroups of G. Prove that if $H_1 \cup H_2$ is also a subgroup of G, then $H_1 \subseteq H_2$ or $H_2 \subseteq H_1$ (or equivalently, if $H_1 \not\subseteq H_2$ and $H_2 \not\subseteq H_1$, then $H_1 \cup H_2$ is not a subgroup of G).
- 6. Prove that if A and B are independent events in a probability space, then A and B^c are also independent.

Note: Please, provide complete arguments everywhere, and explain how you arrived at your answer/solution. Giving the result without explanation leads to score deduction.