Introduction to mathematical cryptography Homework problems Week 11

- 21. Prove that the entropy function has the properties (H1), (H2) and (H3).
- 22. Prove that

$$\lim_{p\to 0+} p\log_2 p = 0.$$

(This statement means that we can add values of zero probability to our random variable: the entropy does not change if we define the terms $0\log_2 0$ to be the above limit, namely, 0.)

Note: Please provide complete arguments everywhere.