Why the Theorem of Scheffé should be rather called a Theorem of Riesz

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In 1947 Henry Scheffé published a result which afterwards became known as Scheffé's theorem, stating that the distributions of a sequence (f_n) of densities, which converge almost surely to a density f, converge uniformly to the distribution of f. But almost 20 years earlier Frigyes Riesz proved a sufficient condition for convergence in the p-th mean $(p \geq 1)$, wherefrom the Scheffé theorem is just a special case.

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